



Fuzzy contra $\theta g'''$ -continuous and irresolute functions in fuzzy topological spaces

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Abstract

In this paper, we introduce a new class of generalized mappings namely fuzzy contra $\theta g'''$ -continuous and fuzzy contra $\theta g'''$ -irresolute mappings in *fts*'s. Some of their properties have been investigated.

Keywords

Fuzzy $\theta g'''$ -continuous, fuzzy contra $\theta g'''$ -continuous and fuzzy contra $\theta g'''$ -irresolute mappings.

AMS Subject Classification

03E72, 54A40.

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Article History: Received 07 December 2020; Accepted 09 February 2021

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1. Introduction

Levine [14] introduced generalized closed sets (*g*-closed sets) in general topology as a generalization of closed sets. Applying the concepts of *g*-closed sets in general topological spaces, several results in general topology were improved by introducing and studying *g*-closed maps by Malghan in 1984 [15] and *g*-continuous maps by Balachandran et al. [2] in 1991. Further generalized preregular closed sets, generalized preregular continuous maps were introduced and studied by Gnanambal [11] in the year 1997 for general topological spaces. Ekici and Kerre [10] introduced fuzzy contra continuous in 2006. In this paper, we have introduced a new class of generalized mappings namely fuzzy $\theta g'''$ -continuous and fuzzy $\theta g'''$ -irresolute mappings in fuzzy topological spaces. Some of their properties have been investigated. As an application of these mappings fuzzy $T_{\theta g'''}$ space, fuzzy $T_{g''' \theta}$ space are introduced and investigated.

2. Preliminaries

Throughout this paper, (P, τ) or simply P mean fuzzy topological space (abbreviated as *fts*). We denote and define the closure and interior for a fuzzy set (briefly, *fs*) λ by

$$fCl(\lambda) = \bigwedge \{ \mu : \mu \geq \lambda, 1 - \mu \in \tau \}$$

$$\text{and } fInt(\lambda) = \bigvee \{ \mu : \mu \leq \lambda, \mu \in \tau \}.$$

Fuzzy θ -closure of λ [9] and fuzzy semi- θ -closure of λ [17] are defined by

$$fCl_{\theta}(\lambda) = \bigwedge \{ fCl(\mu) : \lambda \leq \mu, \mu \in \tau \} \text{ and}$$

$fsCl_{\theta}(\lambda) = \bigwedge \{ fsCl(\mu) : \lambda \leq \mu, \mu \text{ is a fuzzy semi-open (i.e., } \mu \leq fCl(fInt(\mu)) \text{) in } \tau \}$ respectively.

Definition 2.1. A *fs* λ of (P, τ) is called a fuzzy

- (i) θ -closed (briefly, $f\theta c$) [9] if $\lambda = fCl_{\theta}(\lambda)$
- (ii) semi- θ -closed (briefly, $fs\theta c$) [17] $\lambda = fsCl_{\theta}(\lambda)$
- (iii) regular (resp. θ , semi, semi θ & α)-open (briefly, *fro* [1] (resp. *f θo* [9], *fso* [1], *fs θo* [17] & *f αo* [5])) if $\lambda = fInt(fCl(\lambda))$ (resp. $\lambda = fInt_{\theta}(\lambda)$ [9], $\lambda \leq fCl(fInt(\lambda))$, $\lambda = fsInt_{\theta}(\lambda)$ & $\lambda \leq fInt(fCl(fInt(\lambda)))$); *f αCl* (λ) (resp. *fsCl*(λ)) denoted and defined by $\cap \{ \nu : \nu \supseteq \lambda, \nu \text{ is } f\alpha c \text{ (resp. } fs c) \}$.

Definition 2.2. A *fs* λ of (P, τ) is called a fuzzy

- (i) generalized (resp. generalized semi, θ -generalized & θ generalized semi) closed (in short, f_{gc} [3] (resp. f_{gsc} [16], $f_{\theta gc}$ [9] & $f_{\theta gsc}$ [12])) if $fCl(\lambda) \leq v$ (resp. $f_{sCl}(\lambda) \leq v$, $f_{Cl_{\theta}}(\lambda) \leq v$ & $f_{sCl_{\theta}}(\lambda) \leq v$), whenever $\lambda \leq v$ and v is f_{o} set in P .
- (ii) semi (resp. θ -semi) generalized closed (in short, f_{sgc} [4] (resp. $f_{\theta sgc}$ [17])) if $f_{sCl}(\lambda) \leq v$ (resp. $f_{sCl_{\theta}}(\lambda) \leq v$), whenever $\lambda \leq v$ and v is f_{so} set in P .
- (iii) g''' (resp. g^*s & g'''_{α})-closed (briefly, $f_{g'''c}$ [13] (resp. f_{g^*sc} [13] & $f_{g'''_{\alpha}c}$ [13])) if $fCl(\lambda) \leq v$ (resp. $f_{sCl}(\lambda) \leq v$ & $f_{\alpha Cl}(\lambda) \leq v$), whenever $\lambda \leq v$ and v is fuzzy generalized semi open (briefly, f_{gso}) set in P .
- (iv) generalized (resp. generalized semi, θ -generalized, semi generalized, θ -semi generalized, g''' , g^*s , g'''_{α} & θ generalized semi) open set (in short, f_{go} [3] (resp. f_{gso} [16], $f_{\theta go}$ [9], f_{sgo} [4], $f_{\theta sgo}$ [17], $f_{g'''o}$ [13], f_{g^*so} [13], $f_{g'''_{\alpha}o}$ [13] & $f_{\theta gso}$ [12])) if λ^c is f_{gc} (resp. f_{gsc} , $f_{\theta gc}$, f_{sgc} , $f_{\theta sgc}$, $f_{g'''c}$, f_{g^*sc} , $f_{g'''_{\alpha}c}$ & $f_{\theta gsc}$).
- (v) fuzzy $\theta g'''$ (resp. θg^*s , g'''_{θ} , g^*s_{θ} & $g'''_{\alpha}\theta$)-closed [6, 7] (briefly, $f_{\theta g'''c}$ (resp. $f_{\theta g^*sc}$, $f_{g'''_{\theta}c}$, $f_{g^*s_{\theta}c}$ & $f_{g'''_{\alpha}\theta c}$)) set if $f_{Cl_{\theta}}(\lambda)$ (resp. $f_{sCl_{\theta}}(\lambda)$, $fCl(\lambda)$, $f_{sCl}(\lambda)$ and $f_{\alpha Cl}(\lambda)$) $\leq \mu$ whenever $\lambda \leq \mu$ and μ is fuzzy θ generalized semi open (briefly, $f_{\theta gso}$) in X .

Definition 2.3. A function $h : (P, \tau) \rightarrow (Q, \sigma)$ is called a fuzzy

- (i) continuous [8] (in short f_{Cts}) if $h^{-1}(U)$ is a f_{o} set in P , $\forall f_{o}$ set U in Q .
- (ii) g (resp. θ & θg_s)-continuous (in short f_{gCts} [3] (resp. $f_{\theta Cts}$ [17] & $f_{\theta g_s Cts}$ [12])) function if $h^{-1}(U)$ is a f_{gc} (resp. $f_{\theta c}$ & $f_{\theta gsc}$) in P , $\forall f_c$ set U in Q .
- (iii) fuzzy $\theta g'''$ (resp. g'''_{θ} , $g'''_{\alpha}\theta$ & θg^*s)-continuous [6, 7] (briefly, $f_{\theta g'''Cts}$ (resp. $f_{g'''_{\theta}Cts}$, $f_{g'''_{\alpha}\theta Cts}$ & $f_{\theta g^*s Cts}$)) if $h^{-1}(U)$ is a $f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$, $f_{g'''_{\alpha}\theta c}$ & $f_{\theta g^*sc}$) in P for every f_c set U in Q .
- (iv) fuzzy $\theta g'''$ (resp. g'''_{θ})-irresolute [6, 7] (briefly, $f_{\theta g'''Irr}$ (resp. $f_{g'''_{\theta}Irr}$)) if $h^{-1}(V)$ is a $f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$) in $P \forall f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$) V in Q .

Definition 2.4. A function $h : (P, \tau) \rightarrow (Q, \sigma)$ is called a fuzzy contra continuous [10] (in short f_{cCts}) if $h^{-1}(U)$ is a f_c set in P , $\forall f_{o}$ set U in Q .

3. Fuzzy contra $\theta g'''$ -continuous and irresolute functions

Definition 3.1. A function $h : P \rightarrow Q$ is called

- (i) fuzzy contra $\theta g'''$ (resp. g'''_{θ} , $g'''_{\alpha}\theta$ & θg^*s)-continuous (briefly, $f_{c\theta g'''Cts}$ (resp. $f_{cg'''_{\theta}Cts}$, $f_{cg'''_{\alpha}\theta Cts}$ & $f_{c\theta g^*s Cts}$)) if $h^{-1}(\lambda)$ is a $f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$, $f_{g'''_{\alpha}\theta c}$ & $f_{\theta g^*sc}$) in P for every f_{o} set λ in Q .

- (ii) fuzzy contra $\theta g'''$ (resp. g'''_{θ})-irresolute (briefly, $f_{c\theta g'''Irr}$ (resp. $f_{cg'''_{\theta}Irr}$)) if $h^{-1}(\eta)$ is a $f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$) in $P \forall f_{\theta g'''c}$ (resp. $f_{g'''_{\theta}c}$) η in Q .

Theorem 3.2. A function $h : P \rightarrow Q$ is $f_{c\theta g'''Cts}$ iff $\forall f_c$ set, η in Q , $h^{-1}(\eta)$ is a $f_{\theta g'''c}$ in P .

Proof. Let η be any f_c set Q . Since $1 - \eta$ is f_{o} , then by assumption it follows that $h^{-1}(1 - \eta) = 1 - h^{-1}(\eta)$ is $f_{\theta g'''c}$ in P . Converse is similar. \square

Theorem 3.3. (i) Every $f_{c\theta Cts}$ function is a $f_{c\theta g'''Cts}$.

- (ii) Every $f_{c\theta g'''Cts}$ function is a $f_{c\theta g^*sCts}$.

- (iii) Every $f_{c\theta g'''Cts}$ function is a $f_{cg'''_{\theta}Cts}$.
But not conversely.

Proof. Let $h : P \rightarrow Q$ be a $f_{c\theta Cts}$ (resp. $f_{c\theta g'''Cts}$ and $f_{c\theta g^*sCts}$) function. Let λ be a f_{o} set in Q . Since h is a $f_{c\theta Cts}$ (resp. $f_{c\theta g'''Cts}$ and $f_{c\theta g^*sCts}$), $h^{-1}(\lambda)$ is a $f_{\theta c}$ (resp. $f_{\theta g'''c}$ and $f_{\theta g^*sc}$) in P and every $f_{\theta c}$ (resp. $f_{\theta g'''c}$ and $f_{\theta g^*sc}$) set is a $f_{\theta g'''c}$ (resp. $f_{\theta g^*sc}$ and $f_{g'''_{\theta}c}$) in $[6, 7]$, therefore for a f_{o} set λ in Q , $h^{-1}(\lambda)$ is a $f_{\theta g'''c}$ (resp. $f_{\theta g^*sc}$ and $f_{g'''_{\theta}c}$) set in P . Hence h is a $f_{c\theta g'''Cts}$ (resp. $f_{c\theta g^*sCts}$ and $f_{cg'''_{\theta}Cts}$). \square

Example 3.4. Let $P = \{l\} = Q$ and the f_s 's A & B are defined by $A(l) = 0.6$, $B(l) = 0.5$. Consider $\tau = \{0, A, 1\}$ and $\sigma = \{0, B, 1\}$. Then (P, τ) and (Q, σ) are f_{ts} . Then the identity (denoted by, i) $i : (P, \tau) \rightarrow (Q, \sigma)$ is a $f_{c\theta g'''Cts}$ map but not a $f_{c\theta Cts}$, since for the f_{o} set B^c in Q , $i^{-1}(B^c)$ is not a $f_{\theta c}$ but it is a $f_{\theta g'''c}$ set in (P, τ) .

Example 3.5. Let $P = \{l, m\} = Q$ and the f_s 's A , B & K are defined by $A(l) = 0.5$, $A(m) = 0.4$; $B(l) = 0.2$, $B(m) = 0.1$ & $K(l) = 0.1$, $K(m) = 0.2$. Consider $\tau = \{0, A, 1\}$ and $\sigma = \{0, B, 1\}$. Then $h : (P, \tau) \rightarrow (Q, \sigma)$, $h(l) = m$, $h(m) = l$, h is a $f_{c\theta g^*sCts}$ map but not a $f_{c\theta g'''Cts}$, since for the f_{o} set B^c in Q , $h^{-1}(B^c) = K$ is not a $f_{\theta g'''c}$ but it is a $f_{\theta g^*sc}$ set in (P, τ) .

Example 3.6. Let $P = \{p, q\} = Q$ and the f_s 's L , M , R & S are defined by $L(p) = 0.4$, $L(q) = 0.4$; $M(p) = 0.5$, $M(q) = 0.4$; $R(p) = 0.6$, $R(q) = 0.5$ & $S(p) = 0.5$, $S(q) = 0.6$. Consider $\tau = \{0, L, M, 1\}$ and $\sigma = \{0, R, 1\}$. Then $h : (P, \tau) \rightarrow (Q, \sigma)$, $h(p) = q$, $h(q) = p$, is a $f_{cg'''_{\theta}Cts}$ map but not a $f_{c\theta g'''Cts}$, since for the f_{o} set D^c in Q , $h^{-1}(D^c) = S$ is not a $f_{\theta g'''c}$ but it is a $f_{g'''_{\theta}c}$ set in (P, τ) .

Remark 3.7. The following examples shows that the $f_{c\theta g'''Cts}$ function and $f_{c\theta g'''Irr}$ function are independent.

Example 3.8. Let $P = \{u, v\} = Q$ and the f_s 's U , V & W are defined by $U(u) = 0.3$, $U(v) = 0.4$; $V(u) = 0.5$, $V(v) = 0.6$; $W(u) = 0.3$, $W(v) = 0.4$. Consider $\tau = \{0, U, 1\}$ and $\sigma = \{0, V, 1\}$. Then $i : (P, \tau) \rightarrow (Q, \sigma)$ is a $f_{c\theta g'''Cts}$ map but not a $f_{c\theta g'''Irr}$, since for the $f_{\theta g'''c}$ set W in (Q, σ) , $i^{-1}(W)$ is not a $f_{\theta g'''c}$ in (P, τ) .



Example 3.9. Let $P = \{u\} = Q$ and the fs 's U, V & W are defined by $U(u) = 0.3, V(u) = 0.8, W(u) = 0.3$. Consider $\tau = \{0, U, V, 1\}$ and $\sigma = \{0, W, 1\}$. Then $i : (X, \tau) \rightarrow (Y, \sigma)$ is a $fc\theta g'''Irr$ map but not a $fc\theta g'''Cts$, since for the fo set W^c in $Q, i^{-1}(W^c)$, is not a $f\theta g'''c$ in (P, τ) .

Theorem 3.10. The map $g \circ h : P \rightarrow R$ with $h : P \rightarrow Q$ and $g : Q \rightarrow R$, is a

- (i) $fc\theta g'''Cts$ if h is a $fc\theta g'''Cts$ and g is a $fcCts$.
- (ii) $fc\theta g'''Irr$ if h is a $fc\theta g'''Irr$ and g is a $fc\theta g'''Irr$.
- (iii) $fc\theta g'''Irr$ if h is a $fc\theta g'''Irr$ and g is a $fc\theta g'''Cts$.

Definition 3.11. A fts 's P is called fuzzy $T_{\theta g'''}-space$ (briefly $fT_{\theta g'''}s$) [6, 7] if every $f\theta g'''c$ set in P is a fc set.

Theorem 3.12. Let P be any fts and Q be $fT_{\theta g'''}s$ and $h : P \rightarrow Q$ be a $fc\theta g'''Irr$ function. Then h is a $fc\theta g'''Cts$.

Proof. Obvious. □

Theorem 3.13. Let $h : P \rightarrow Q$ be a $fc\theta g'''Cts$ with P (resp. Q) be a $fT_{\theta g'''}s$, then h is a $fcCts$ (resp. $fc\theta g'''Irr$).

Theorem 3.14. The map $g \circ h : P \rightarrow R$ is a $fc\theta g'''Cts$, if $h : P \rightarrow Q$ is a $f\theta g'''Cts$ and $g : Q \rightarrow R$ is a $fc\theta g'''Cts$ with Q as a $fT_{\theta g'''}s$.

Proof. Since g is $fc\theta g'''Cts, g^{-1}(\lambda)$ is a $f\theta g'''c$ set in $Q \forall fo, \lambda$, in R . Since Q is a $fT_{\theta g'''}s, g^{-1}(\lambda)$ is a fc in Q implies $h^{-1}(g^{-1}(\lambda)) = (g \circ h)^{-1}(\lambda)$ is $f\theta g'''c$ set in P . Hence a $g \circ h$ is a $fc\theta g'''Cts$. □

Theorem 3.15. A function $h : P \rightarrow Q$ is a $fcg'''\theta Cts$ iff the inverse image of each fc set in Q is a $fcg'''\theta o$ in P .

Theorem 3.16. Every

- (i) $fcCts$ function is a $fcg'''\theta Cts$.
- (ii) $fcg'''\theta Cts$ function is a $fcg'''_{\alpha}\theta Cts$.
- (iii) $fcg'''\theta Irr$ function is a $fcg'''\theta Cts$.

But not conversely.

Proof. We prove only (i) and (ii). Suppose $h : P \rightarrow Q$ be a $fcCts$ (resp. $fcg'''\theta Cts$). Then $h^{-1}(\lambda)$ is fc (resp. $fcg'''\theta c$) $\forall fo, \lambda$ in Q . Since every fo (resp. $fcg'''\theta o$) set is a $fcg'''\theta o$ (resp. $fcg'''_{\alpha}\theta o$), for a fo set λ in $Q, h^{-1}(\lambda)$ is a $fcg'''\theta c$ (resp. $fcg'''_{\alpha}\theta c$) set in P . Hence h is a $fcg'''\theta Cts$ (resp. $fcg'''_{\alpha}\theta Cts$). □

Example 3.17. Let $P = \{p, q\} = Q$ and the fs 's L, M, R & S are defined by

$$\begin{aligned} L(p) &= 0.4, L(q) = 0.4; \\ M(p) &= 0.5, M(q) = 0.4; \\ R(p) &= 0.3, R(q) = 0.4; \end{aligned}$$

$$S(p) = 0.6, S(q) = 0.7.$$

Consider $\tau = \{0, L, M, 1\}$ and $\sigma = \{0, R, 1\}$. Then (P, τ) and (Q, σ) are fts . Define $h : (P, \tau) \rightarrow (Q, \sigma)$ as $h(p) = q, h(q) = p$. Then h is a $fcg'''\theta Cts$ map but not a $fcCts$, since for the fo set R^c in $Q, h^{-1}(R^c) = S$ is not a fc but it is a $fcg'''\theta c$ set in (P, τ) .

Example 3.18. Let $P = \{u\}$ and the fs 's U, V & W are defined by $U(u) = 0.5; V(u) = 0.3; W(u) = 0.4$. Consider $\tau = \{0, U, V, 1\}$ & $\sigma = \{0, W, 1\}$. Then $i : (P, \tau) \rightarrow (Q, \sigma)$ is a $fcg'''_{\alpha}\theta Cts$ map but not a $fcg'''\theta Cts$, since for the fo set W^c in $Q, i^{-1}(W^c) = W^c$ is not a $fcg'''\theta c$ but it is a $fcg'''_{\alpha}\theta c$ set in (P, τ) .

Example 3.19. Let $P = \{u, v\} = Q$ and the fs 's U, V & W are defined by

$$\begin{aligned} U(u) &= 0.3, U(v) = 0.3; \\ V(u) &= 0.6, V(v) = 0.5; \\ W(u) &= 0.6, W(v) = 0.6. \end{aligned}$$

Consider $\tau = \{0, U, 1\}$ & $\sigma = \{0, V, 1\}$. Then $i : (P, \tau) \rightarrow (Q, \sigma)$ is a $fcg'''\theta Cts$ map but not a $fcg'''\theta Irr$, since for the $fcg'''\theta o$ set W in $(Q, \sigma), i^{-1}(W)$ is not a $fcg'''\theta c$ in (P, τ) .

Theorem 3.20. The map $g \circ h : P \rightarrow R$ with $h : P \rightarrow Q$ and $g : Q \rightarrow R$, is a

- (i) $fcg'''\theta Cts$ if h is a $fcg'''\theta Cts$ & g is a $fcCts$.
- (ii) $fcg'''\theta Irr$ if h is a $fcg'''\theta Irr$ & g is a $fcg'''\theta Irr$ functions.
- (iii) $fcg'''\theta Cts$ if h is a $fcg'''\theta Irr$ & g is a $fcg'''\theta Cts$ functions.

Definition 3.21. A fts 's P is called fuzzy $T_{g'''}\theta$ -space (briefly $fT_{g'''}\theta s$) if every $fcg'''\theta c$ (resp. $fcg'''\theta o$) set in P is a fc (resp. fo) set.

Theorem 3.22. Let P be any fts & Q be a $fT_{g'''}\theta s$ and $h : P \rightarrow Q$ be $fcg'''\theta Irr$ function. Then h is a $fcg'''\theta Cts$.

Proof. Obvious. □

Theorem 3.23. Every $fT_{\theta g'''}s$ is a $fT_{g'''}\theta s$.

Proof. Let X be a $fT_{\theta g'''}s$ and let λ be a $f\theta g'''c$ set in X . Then by definition, λ is a fc set in P . Since every $f\theta g'''c$ set is a $fcg'''\theta c$ set. Thus λ is a $fcg'''\theta c$ in P . Hence P is a $fT_{g'''}\theta s$. □

Theorem 3.24. Let $h : P \rightarrow Q$ be a $fcg'''\theta Cts$ & P (resp. Q) be a $fT_{g'''}\theta s$, then h is a $fcCts$ (resp. $fcg'''\theta Irr$).

Proof. Obvious. □

Theorem 3.25. If $h : P \rightarrow Q$ is $fcg'''\theta Cts$ & $g : Q \rightarrow R$ is $fcg'''\theta Cts$ & Q be a $fT_{g'''}\theta s$, then $g \circ h : P \rightarrow R$ is a $fcg'''\theta Cts$.



Proof. Suppose g is a $fg'''\theta Cts$, then $g^{-1}(\lambda)$ is a $fg'''\theta c$ in Q , $\forall fc \lambda$ in R . Since Q is a $fT_{g'''\theta s}$, $g^{-1}(\lambda)$ is fc in Q . Also since $h : P \rightarrow Q$ is $fcg'''\theta Cts$, $h^{-1}(g^{-1}(\lambda))$ is a $fg'''\theta o$ in P . i.e., $h^{-1}(g^{-1}(\lambda)) = (g \circ h)^{-1}(\lambda)$ is a $fg'''\theta o$ set in P . \square

Theorem 3.26. Let $h : P \rightarrow Q$ be an onto, $fcg'''\theta Irr$ & a fc map. If P is a $fT_{g'''\theta s}$ then Q is also a $fT_{g'''\theta s}$.

Proof. Let λ , in Q , be a $fcg'''\theta o$. $h^{-1}(\lambda)$, in P , is a $fg'''\theta c$ set, since h is a $fcg'''\theta Irr$. Also since P is a $fT_{g'''\theta s}$, $h^{-1}(\lambda)$ is a fc in P . And so $h(h^{-1}(\lambda)) = \lambda$ is a fc in Q as h is both fc and onto function. Hence Q is a $fT_{g'''\theta s}$. \square

Theorem 3.27. Let $h : P \rightarrow Q$ be an onto, $fc\theta g''' Irr$ & a fc map. If P is a $fT_{\theta g'''\theta s}$ then Q is also a $fT_{\theta g'''\theta s}$.

Proof. Let λ , in Q , be a $f\theta g''' o$. $h^{-1}(\lambda)$, in P , is a $f\theta g''' c$ and fc , since h is a $f\theta g''' Irr$ and $fT_{\theta g'''\theta s}$. And so $h(h^{-1}(\lambda)) = \lambda$ is a fc in Q as h is both fc and onto function. Hence Q is a $fT_{\theta g'''\theta s}$. \square

Conclusion

In this paper, we introduced a new class of generalized mappings in a contra part namely fuzzy contra $\theta g'''$ -continuous and fuzzy contra $\theta g'''$ -irresolute mappings in fts 's. Further, some of their properties in contra mappings have been investigated. Also, an application of these mappings fuzzy $T_{\theta g'''\theta}$ -space, fuzzy $T_{g'''\theta}$ -space are introduced and investigated in fts . These can be carried out to open mappings and closed mappings in their future work.

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ISSN(P):2319 – 3786

Malaya Journal of Matematik

ISSN(O):2321 – 5666

